



Cambridge International AS & A Level

CANDIDATE NAME				
CENTRE NUMBER		CANDIDATE NUMBER		

MATHEMATICS 9709/22

Paper 2 Pure Mathematics 2

February/March 2025

1 hour 15 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

This document has 12 pages.

	* 0000800000002 *
1	Solve the equation $ln(3x+1) - ln(x-1)$

1	Solve the equation $\ln(3x+1) - \ln(x-5) = \ln 7$.

Solve the equation $\ln(3x+1) - \ln(x-5) = \ln 7$.	[3
	••••••
	•••••



	A curve passes through the point with coordinates $\left(\frac{1}{2}\pi, 5\right)$ and is such that $\frac{dy}{dx} = 4\sec^2\left(\frac{1}{2}x\right)$.
	Find the equation of the curve.
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The diagram shows the curves $y = e^{2x}$ and $y = 8e^{-x}$. The shaded region is bounded by the two curves and the y-axis.

(b) Find the area of the shaded region.	[3]



A curve has equation $y = \frac{4 \sin x}{3 + \cos 2x}$ for values of x such that $0 \le x \le 2\pi$.

(a)	Find $\frac{dy}{dx}$.	[2]
(b)	Hence find the coordinates of the stationary points of the curve.	[4]

DO NOT WRITE IN THIS MARGIN

The x-coordinates of the points where the graphs intersect are denoted by α and β , where $\alpha < \beta$.

(b)	Show that $\alpha = 1.5 - 0.5 \ln(\alpha + 1)$.	[1
		•••••
		•••••
(c)	Use an iterative formula, based on the equation in part (b), to find the value of α corre	ect to
	3 significant figures. Give the result of each iteration to 5 significant figures.	Г3

• • • • •

(d)	Show by calculation that $2.055 < \beta < 2.065$.	[2]
		••••



* 0000800000007 *	

(a)	Find the quotient and remainder when $18x^3 - 6x^2 - 30x + 4$ is divided by $(3x - 1)$.
(b)	Hence find $\int_{1}^{5} \frac{18x^3 - 6x^2 - 30x + 4}{3x - 1} dx$. Give your answer in the form $a - \ln b$, where a and b and
	integers.

correct to 2 decimal places.	
 	•••••

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	Hence solve the equation $6 \sin \theta - 4 \cos \theta + 5 = 0$ for $0^{\circ} < \theta < 360^{\circ}$.
	As the value of B varies find the greatest nossible value of
,	As the value of β varies, find the greatest possible value of
	$(3\sin 4\beta - 2\cos 4\beta)^2 + 15$
	$(3\sin 4\beta - 2\cos 4\beta)^2 + 15$
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(a)

8 A curve has equation $3e^{2x}y + 4e^{3x} + y^3 = 18$.

Show that $\frac{dy}{dx} = \frac{-2e^{2x}y - 4e^{3x}}{e^{2x} + y^2}.$	[4]
$dx \qquad e^{2x} + y^2$	
	••••••
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(b)	Show that the curve has no stationary points.		

Additional page

12

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